

Fibonacci Numbers and Golden Ratio



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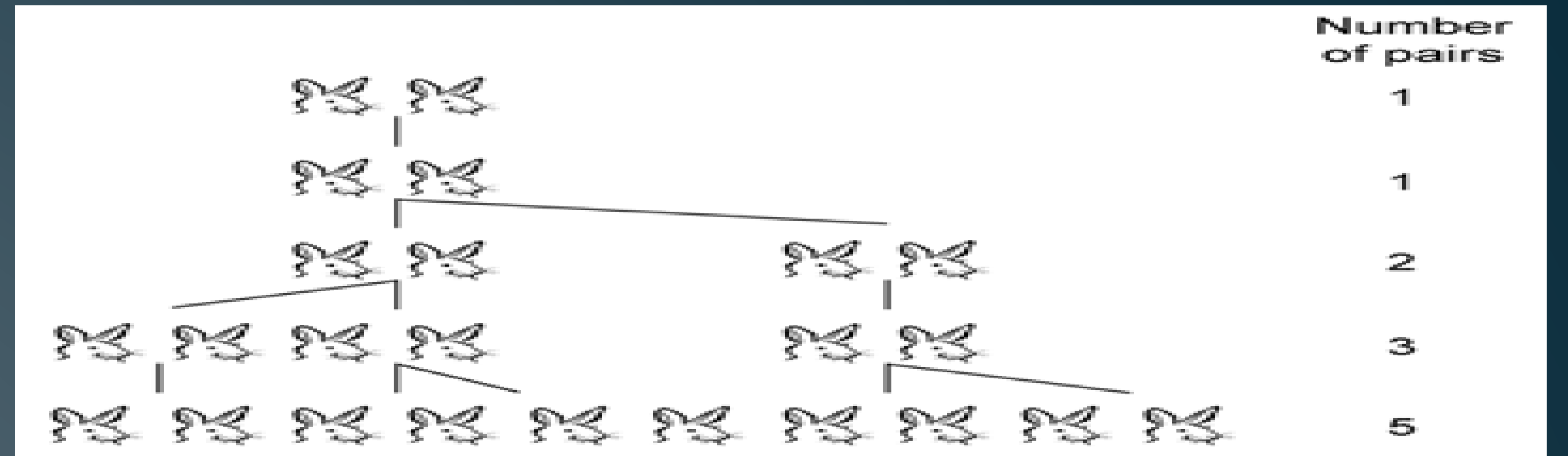
0 1 1 2 3 5 8 13 21 34

GENERAL FORMULA : $F_{n+2} = F_{n+1} + F_n$

This series was developed by
“LEONARDO PISANO”
 also known as **“FIBONACCI”**

The first two numbers in the Fibonacci sequence are either 1 and 1 or in modern usage 0 and 1.

- Fibonacci applied his sequence to a problem involving the breeding of rabbits
- He mapped out the family tree of a group of rabbits that initially started with only two members
- The number of rabbits at any given time was always a Fibonacci number



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$13 \div 8 = 1.625$

$21 \div 13 = 1.615...$

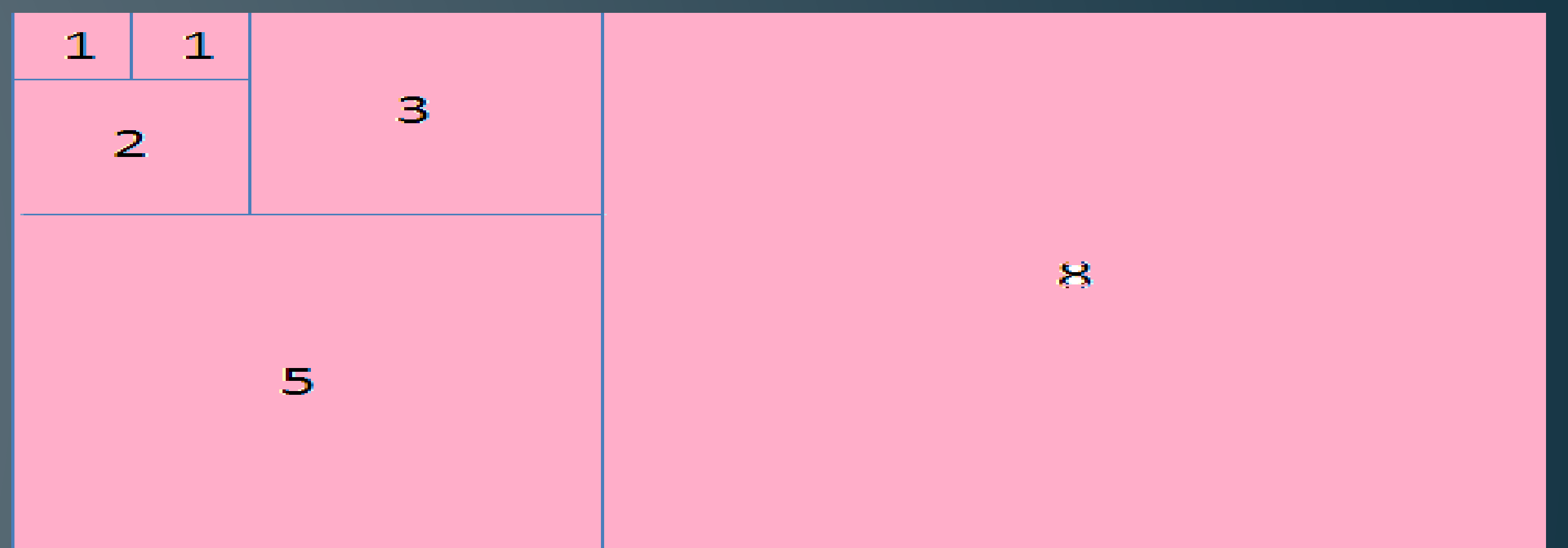
$34 \div 21 = 1.619...$

$55 \div 34 = 1.6176...$

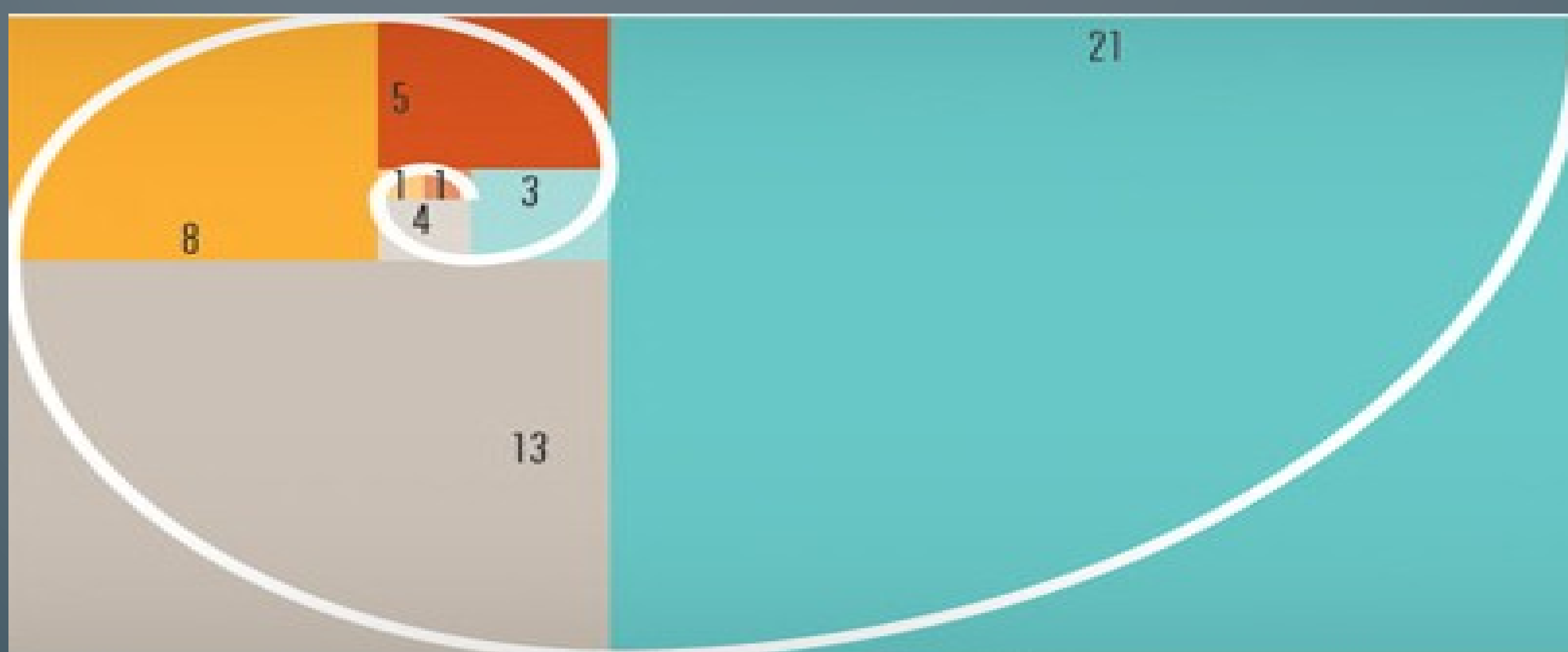
$89 \div 55 = 1.61818...$

The Golden Ratio:
1.618033....

- “JOHANNES KELPER” observed that the ratio of consecutive Fibonacci numbers converges
- He wrote that as “5:8 so is 8:13”, practically and as 8:13, so is “13:21 almost”
- He concluded that the limit approaches the beautiful number known as “GOLDEN RATIO”



- A rectangle whose sides are in the golden ratio is referred to as a “GOLDEN RECTANGLE”.
- When a golden rectangle is squared, the remaining area forms another golden rectangle.
- Area of the rectangle = $1^2 + 1^2 + 2^2 + 3^2 + 5^2 + 8^2 = 8 * (5 + 8)$



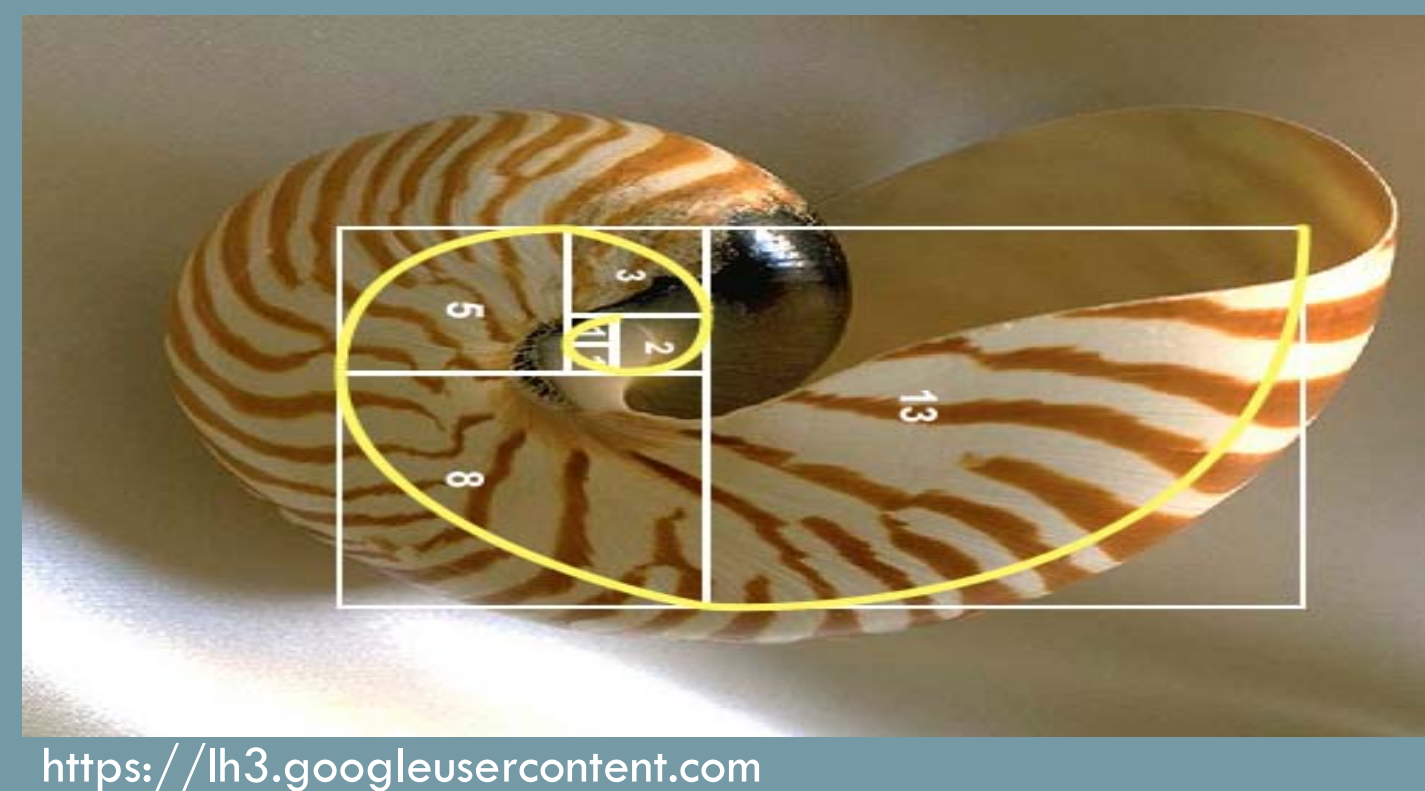
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- A golden spiral is a spiral whose growth factor is ϕ , the golden ratio.
- That is, a golden spiral gets wider (or further from its origin) by a factor of ϕ for every quarter turn it makes.

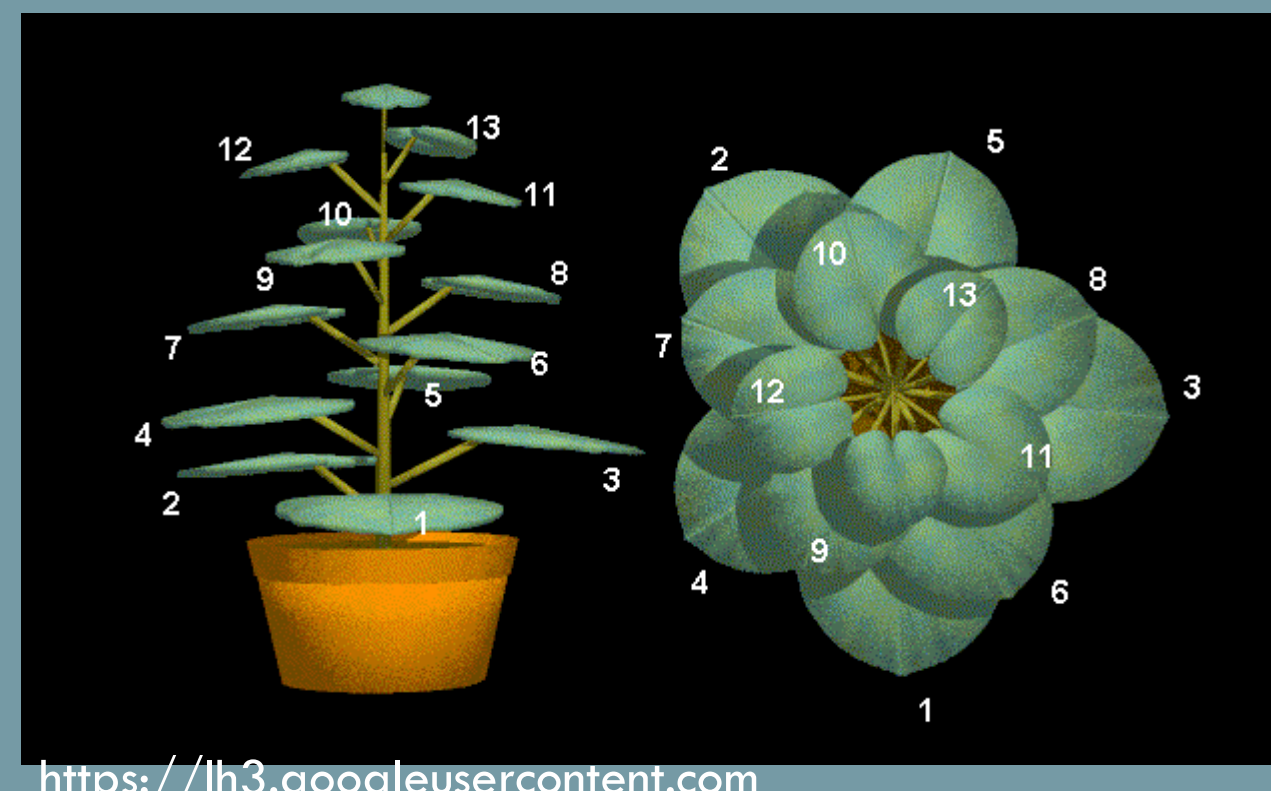
Nature also uses Fibonacci Series and Golden Ratio in its designs



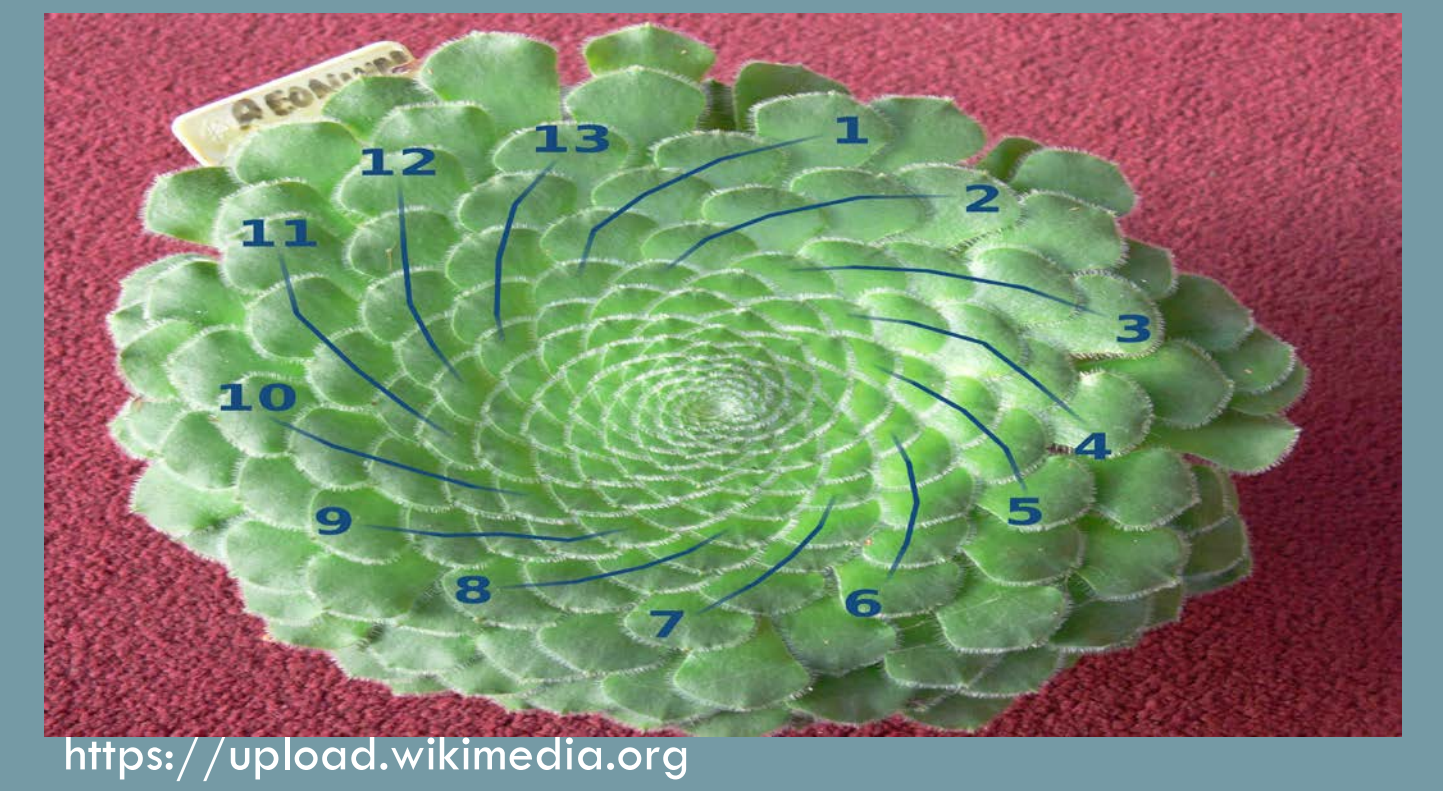
Each section of index finger, from the tip to the base of the wrist is larger than the preceding one by about Fibonacci numbers.



Snail shells follow golden spiral



Leaves and branching of plants always branch off into groups of Fibonacci Numbers



The head of a flower is also subject to Fibonacci Processes. It has 13 spirals..

1 1 2 3 5 8 13 21 34 55 ...
 1 1 4 9 25 64 169 441 1156 3025 ...

$1 + 1 + 4 = 6 = 2 \times 3$

$1 + 1 + 4 + 9 = 15 = 3 \times 5$

$1 + 1 + 4 + 9 + 25 = 40 = 5 \times 8$

$1 + 1 + 4 + 9 + 25 + 64 = 104 = 8 \times 13$

$1^2 + 1^2 + 2^2 + 3^2 + 5^2 + 8^2 = 8 \times 13$

Why?

Interesting fact about Fibonacci Series:

In Fibonacci series, if we consider the square of each term then we find a very interesting result, that is-
 The sum of squares of n consecutive terms is equal to the product of n^{th} and $(n+1)^{th}$ term.

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